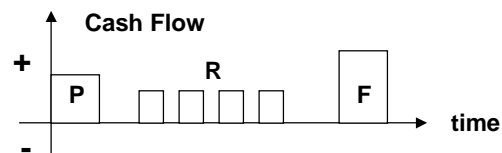


Engineering Economy

- **Objective:**
 - To provide economic comparison of benefits and costs that occur over time
- **Assumptions:**
 - All Benefits, Costs measured in money
 - Single point of view



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Issue - Value over time

- Money now has a different value than the same amount at a different date
- Comparable to }
not equal to } interest rate
- Proper name: Discount Rate, r
(because future benefits/costs are reduced to compare with present)

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Formulas for N Periods

- **Single amounts**

a) Future Amount = $P (1 + r)^N = P (\text{caf})$
caf = Compound Amount Factor

b) Present Amount = F/caf
 $1/\text{caf}$ = Present Worth Factor

- **Finite Series**

c) $F = \sum_i R (1 + r)^i = R [(1 + r)^N - 1] / r$

d) $R = P (\text{crf}) = [P * r (1 + r)^N] / [(1 + r)^N - 1]$
crf = Capital Recovery Factor

Formulas for N Periods (cont')

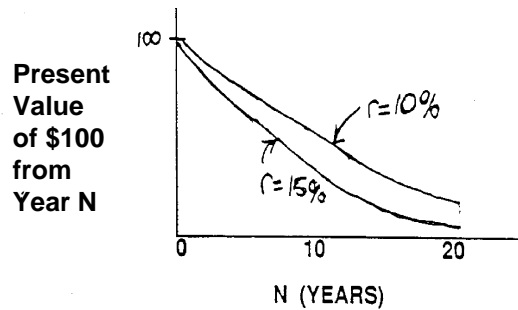
- **Infinite Series**

$1 \ll (1 + r)^N \Rightarrow (1 + r)^N / [(1 + r)^N - 1] \rightarrow 1 \Rightarrow \text{crf} \rightarrow r$

- **Small Periods**

$(1 + r)^N \rightarrow e^{rN}$

Effect of Different Discount Rates



- Higher $r = >$ smaller value of future benefits; discourages projects whose benefits pay back costs over long time. Advocates of projects try to minimize so projects look good!

Discount Rate Approximation

- To appreciate effect of discounting:
“Rule of 72” or “Rule of 70”
 $e^{rN} = 2.0$ when $rN = 0.72$ (actually = 0.693)
- Therefore, present amount doubles when future amount halves
 $rN = 72$ with r expressed in percent
- Examples
 - When would \$1000 invested at 10% double?
 - What is, at 9%, the value of \$1000 in 8 years?